Name:

Instructions for Doing These Problems:

- 1. When you first attempt the problem, **DO NOT** use any help (books, notes, etc)
- 2. If you cannot solve the problem during step 1, then you may use books and notes. If you solve it during this step, make a special mark next to the problem number and make sure to review that section.
- 3. If you cannot solve it during step 2, then I recommend either asking me or a classmate for help. Make sure to mark the problem and read the section.
- 4. Once you've finished all of the problems, you should focus on practice problems from the corresponding sections of your marked problems. I **highly recommend** doing odd-numbered exercises until you're almost always getting the right answer with no help.

1. Evaluate the integral
$$\int_0^{\sqrt{2}} \int_x^{\sqrt{4-x^2}} x^2 + y^2 \, dy \, dx$$
.

2. Evaluate the integral $\iint_D y \, dA$ where D is the region bounded by $x^2 + y^2 = 1$ and y = |x|.

3. Sketch the solid whose volume is represented by the integral:

$$\int_0^{\frac{\pi}{2}} \int_1^3 r^2 \sin(\theta) \, dr \, d\theta$$

4. Evaluate the sum of integrals:

$$\int_{\frac{-3}{\sqrt{2}}}^{0} \int_{-\sqrt{9-y^2}}^{y} yx^3 \, dx \, dy + \int_{0}^{3} \int_{-\sqrt{9-y^2}}^{\sqrt{9-y^2}} yx^3 \, dx \, dy$$

5. Calculate the mass of the lamina with density $\rho(x, y) = x^2$ and shape bounded by $x = y^2$ and x = 4. 6. Calculate the x-coordinate of the center of mass of the lamina with density $\rho(x,y) = \frac{y}{x}$ and shape bounded by the vertices (1,1), (2,0), (1,0).

7. Set up the integral for the mass of the object with density $\rho(x, y, z) = x + y$ and shape in the first octant bounded by z = 5, x = 2, and y = 10 - x - z.

8. Find the surface area of the surface defined by the parametrization $\vec{r}(u,v) = \langle u-v, 3+v+u, u \rangle$ where $0 \le u \le 2$ and $-1 \le v \le 1$.

9. Find the surface area of the surface defined by $f(x,y) = x^2 - y^2$ where $x^2 + y^2 \le 1$.

10. Find the surface area of the elliptic paraboloid $x = y^2 + z^2$ within the sphere $x^2 + y^2 + z^2 = 6$.

11. Find the volume of the solid in the 1st octant bounded between the planes z = 4-xand y = 2 - x. 12. Set up, but do not evaluate, $\iiint_E e^y dV$ where E is the region bounded by $x = y^2$, $z = 16 - x^2$, and z = 0.

13. Sketch the solid whose volume is given by

$$\int_{-1}^{1} \int_{-1}^{1} \int_{-1}^{e^{x+y}} 1 \, dz \, dx \, dy$$

14. Let f(x, y, z) be an arbitrary continuous function. Switch the order of integration of

$$\int_{-2}^{2} \int_{0}^{\sqrt{4-x^2}} \int_{0}^{2-x} f(x,y,z) \, dz \, dy \, dx$$

to $dy \, dx \, dz$.

15. Evaluate the integral $\iiint_E z + 2 \, dV$ where *E* is the region inside the cylinder $x^2 + z^2 = 25$ and bounded by the planes y = x + 5 and y = x - 5.

16. Evaluate the integral $\iiint_E x^2 + y^2 dV$ where *E* is the region beneath the cone $z = \sqrt{x^2 + y^2}$ and inside the sphere $x^2 + y^2 + z^2 = 36$.

17. Sketch the region whose volume is represented by the integral

$$\int_0^{\pi} \int_{-1}^2 \int_0^{\sqrt{1+z^2}} r \, dr \, dz \, d\theta.$$

18. Find the volume of the region outside the cylinder $x^2 + y^2 = 1$ and inside the sphere $x^2 + y^2 + z^2 = 4$.

19. Sketch the region T(R) where R is the rectangle with vertices (0,0), (1,0), (0,1), (1,1)and T is the transformation $T(u,v) = \langle u+v, \sqrt{u} \rangle$

20. Evaluate the integral $\iint_D \frac{x-2y}{x^2+y^2+2xy+1} dA$ where D is the region bounded by y = 1-x, x+y = 2, x = 2y and $x-2y = \sqrt{x+y}$ using the transformation $T(u, v) = \left\langle \frac{u+2v}{3}, \frac{v-u}{3} \right\rangle$

21. Evaluate the integral $\iint_D x e^{x^2 - y^2} + y e^{x^2 - y^2} dA$ where D is the region bounded by $|x| + |y| \le 2$.

22. Evaluate $\int_C xy \, ds$ where C is the section of the circle $x^2 + y^2 = 1$ starting at (0, -1) and going to (0, 1).

23. Evaluate $\int_C \mathbf{F} \cdot d\mathbf{r}$ where $\mathbf{F}(x, y) = \langle -y, x \rangle$ and C is the line segment connecting (-1, -1) to (2, 2).

24. Evaluate $\int_C y^2 ds$ where C is given by $\mathbf{r}(t) = \langle 2\cos(t), 2, 2\sin(t) \rangle$ where $0 \le t \le 2\pi$.

25. Evaluate $\int_C \mathbf{F} \cdot d\mathbf{r}$ where $\mathbf{F}(x, y) = \langle y, -x \rangle$ and C is the path that starts at (-1, 0), goes to (1, 0) clockwise, then travels back to (-1, 0) along the x-axis.