Name:

Instructions for Doing These Problems:

- 1. When you first attempt the problem, **DO NOT** use any help (books, notes, etc)
- 2. If you cannot solve the problem during step 1, then you may use books and notes. If you solve it during this step, make a special mark next to the problem number and make sure to review that section.
- 3. If you cannot solve it during step 2, then I recommend either asking me or a classmate for help. Make sure to mark the problem and read the section.
- 4. Once you've finished all of the problems, you should focus on practice problems from the corresponding sections of your marked problems. I **highly recommend** doing odd-numbered exercises until you're almost always getting the right answer with no help.
- 1. Find the domain of $f(x, y) = \sqrt{y} \ln(x 4)$.

2. Find the domain of $g(x, y) = \frac{x^2 - xy + y^2}{\sin(\pi xy)}$.

3. Describe the level surfaces of the function $h(x, y) = x^2 - y^2$.

4. Describe the level surfaces of the function $\sigma(x,y) = \ln(x^2 + y^2)$

5. Determine whether or not the following limit exists. If it does, calculate the limit:

$$\lim_{(x,y)\to(0,0)}\frac{x}{x+y}$$

6. Determine whether or not the following limit exists. If it does, calculate the limit:

$$\lim_{(x,y)\to(0,0)}\frac{3xy}{2x^2+2y^2}$$

7. Determine whether or not the following limit exists. If it does, calculate the limit:

$$\lim_{(x,y)\to(0,0)}\frac{xy^3}{x^2+y^6}$$

8. Determine whether or not the following limit exists. If it does, calculate the limit:

$$\lim_{(x,y)\to(0,0)}\frac{xe^y}{x+y}$$

9. Find the value c to make this function continuous everywhere. If no c exists, then explain why:

$$f(x,y) = \begin{cases} \frac{x^2 + y^2}{\sqrt{x^2 + y^2 + 1} - 1} & (x,y) \neq (0,0) \\ c & (x,y) = (0,0) \end{cases}$$

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$$f(x,y) = \begin{cases} \frac{x^2 + 2y^2}{\sqrt{x^2 + y^2}} & (x,y) \neq (0,0) \\ c & (x,y) = (0,0) \end{cases}$$

11. Calculate the partial derivatives of $f(x, y) = xy - 3e^y$

12. Calculate the partial derivatives of $g(w, x, y, z) = wx^3 - \cos(xyz) + 3w^2 \ln(yz)$

13. Calculate the partial derivatives of $\vec{h}(x, y, z) = \langle x \tan(x) - y, yz + z^4, xyz + 4ye^{xy} \rangle$

14. Find the equation of the tangent plane to the surface $f(x, y) = \sin(xy) + x$ at the point (0, 1).

15. Find the equation of the tangent plane to the surface $f(x, y) = xy - x^2 + y$ at the point (-3, 2)

16. Find the equation of the tangent plane to the surface $\vec{r}(t,s) = \langle s-t^2, \sin(t), t^3+s^3 \rangle$ when t = 0 and s = 4.

17. Find the equation of the tangent plane to the surface $\vec{r}(t,s) = \langle t^3 + 2t^2 - st + 5, s^2t, t-s \rangle$ at the point (8,0,1).

18. Use linearization to estimate the value of f(.9, .9) where $f(x, y) = ye^{x-1}$.

19. Use linearization to estimate the value of $e^{.1}\cos(3)$

20. Let z = f(x, y) with x and y as functions of s and t given by $x(s, t) = s^2 - t$ and $y(s, t) = \frac{t}{s}$. Calculate the partials of f with respect to s and t.

21. Let z = f(x, y, w) with x, y, and w as functions of s and t given by $x(s, t) = e^t$ and $y(s,t) = s^3 - s$ and $w(s,t) = s^4 - \sin(ts)$. Calculate the partials of f with respect to s and t.

22. Let z = f(x, y) with x and y as functions of s, t, u, and v given by $x(s, t, u, v) = uv - e^{st}$ and $y(s, t, u, v) = \cos(u)\cos(v)$. Calculate the partials of f with respect to s, t, u, and v.

23. Calculate the directional derivative of $f(x, y) = x^3 + xy - 4$ in the direction of $\vec{u} = \langle 1, 0 \rangle$ at the point (1, 1).

24. Calculate the directional derivative of $f(x, y) = y^2 - x^3 y$ in the direction of $\vec{u} = \langle 2, 1 \rangle$ at the point (-2, 3).

25. Calculate the maximum rate of change of $f(x, y) = e^x + xy^2$ at the point (0, 3).

26. Determine the direction of the maximum rate of change of $f(x, y) = \sin(xy)$ at the point $(\pi, 2)$.

27. Determine the equation of the tangent plane to the surface $x^2 - y^2 - 2z^2 = 4$ at the point (4, 2, 2).

28. Calculate the equation of the normal line to the surface $x^2 + y^2 + z^2 = 1$ at the point (1, 0, 0).

29. Find and classify the local extrema of $f(x, y) = x^2 - 3y^2 + 1$

30. Find and classify the local extrema of $f(x, y) = x^2y - x - y^2$

31. Find and classify the local extrema of $f(x, y) = x^4 + y^2 x - xy$

32. Find and classify the absolute extrema of $f(x, y) = x^2 + 2y^2 - 3$ on the disk $D = \{(x, y) | x^2 + y^2 \le 3\}.$

33. Calculate the maximum and minimum values attained by $f(x,y) = xy^2$ under the constraint $x^2 + y^2 = 3$

34. Calculate the maximum and minimum values attained by f(x, y, z) = xyz under the constraint $x^2 + y^2 + z^2 = 1$.

35. Calculate two points on the circle $x^2 + y^2 = 4$: the point furthest from (3,3) and the point closest to (3,3).

36. Describe the object whose volume can be interpreted as the double integral

$$\iint_R 10 \, dA$$

where $R = [0, 1] \times [-5, 2]$.

37. True/False: The integral

$$\iint_R \sqrt{1-x^2} \, dA$$

where $R = [-1, 1] \times [-1, 1]$, represents the volume of the upper half-sphere of radius 1.

38. Estimate the double integral $\iint_R x^2 - y^2 dA$ where $R = \{(x, y) \mid -4 \le x \le 2, 2 \le y \le 4\}$ using 3 rectangles of equal area.

39. Evaluate the double integral $\iint_R x^4 (1+y)^3 dA$ where $R = [0,3] \times [0,5]$.

40. Evaluate the double integral $\iint_R x e^{xy} dA$ where $R = [-3, 1] \times [7, 9]$.

41. Evaluate the double integral $\iint_R \ln(x) y \, dA$ where $R = [4, 5] \times [-1, 1]$.

42. Evaluate the double integral $\iint_D 5x^2y \, dA$ where D is the region bounded by $y = 4 - x^2$ and the x-axis.

43. Evaluate the double integral $\iint_D \cos(x^2) dA$ where D is the region bounded by y = x, x = 4 and the x-axis.

44. Evaluate the double integral $\iint_D x e^y dA$ where D is the region bounded by $y = \ln(x), x = 3$, and the x-axis.

45. Evaluate the double integral $\iint_D \frac{y}{1+x^2} dA$ where D is the region bounded by x = -1, x = 1, y = 0 and y = 8.