Name:

Instructions for Doing These Problems:

- 1. When you first attempt the problem, **DO NOT** use any help (books, notes, etc)
- 2. If you cannot solve the problem during step 1, then you may use books and notes. If you solve it during this step, make a special mark next to the problem number and make sure to review that section.
- 3. If you cannot solve it during step 2, then I recommend either asking me or a classmate for help. Make sure to mark the problem and read the section.
- 4. Once you've finished all of the problems, you should focus on practice problems from the corresponding sections of your marked problems. I **highly recommend** doing odd-numbered exercises until you're almost always getting the right answer with no help.
- 1. Find the distance between the points (1, 2, 3) and (-1, -2, 0).

2. Find the distance between the center of the sphere $(x-3)^2 + (y+1)^2 + z^2 = 9$ and the point (0, 9, -3).

3. Sketch the graph of the equation $y^2 + z^2 = 1$ in \mathbb{R}^3 .

4. Find the dot product of the vectors $\langle -1, 1, -1 \rangle$ and $\langle 2, 10, -3 \rangle$.

5. Determine whether the vectors $\langle 2,-1,1\rangle$ and $\langle 3,3,-3\rangle$ are orthogonal.

6. Find the angle between the vectors $\langle 3, 0, -2 \rangle$ and $\langle -1, -1, -1 \rangle$.

7. Compute the scalar projection of $\langle 2,0,4\rangle$ on $\langle 4,0,0\rangle.$

8. Sketch the vector projection of (3, 1, 2) on (1, 1, 0) along with the vectors (3, 1, 2) and (1, 1, 0).

9. Find a vector perpendicular to both (0, -2, 5) and (1, 0, 1).

10. Determine whether the vectors $\langle 12, 4, 15 \rangle$ and $\langle 3, 1, 4 \rangle$ are parallel.

11. Calculate the area of the parallelogram formed by the vectors $\langle 7, 3, -2 \rangle$ and $\langle 0, 19, -1 \rangle$.

12. Calculate the volume of the parallelepiped formed by the vectors $\langle 2, -2, -1 \rangle$, $\langle -1, -1, 1 \rangle$, and $\langle 3, 2, 5 \rangle$.

13. Determine whether or not the vectors $\langle -1, 0, 3 \rangle$, $\langle 4, 1, 2 \rangle$, and $\langle -3, -1, 2 \rangle$ lie on the same plane.

- 14. Write the equation of the line $\frac{x-2}{3} = \frac{y}{4} = z + 2$ in parametric form.
- 15. Write the equation of the line $\langle t+1, -3t+4, 7t-2 \rangle$ as symmetric equations.
- 16. Write the equation of the line that goes through the point (0, 0, 3) and has direction vector $\langle 4, -2, -1 \rangle$.

17. Write the equation of the line that goes through the points (-5, 1, 0) and (0, -2, -5).

18. Determine whether the points (1, 1, 1), (2, 3, -4) and (-1, -3, 4) lie on the same line.

19. Find the equation of the plane with normal vector (6, 2, 5) and point on the plane (0, 0, -1).

20. Find the equation of the intersection of the planes x + y + z = 1 and -x - 2z = 4.

21. Find the equation of the plane containing the lines $\langle t, 9-t, 2t \rangle$ and $\frac{x}{2} = y = z+4$.

22. Find the angle between the planes 2x - y = 6 and 3y + 2z = -2.

23. Find the equation of the plane containing the points (0, 0, -3), (1, 2, 0), and (7, 1, 1).

24. Find the equation of a plane parallel to the plane containing the points (0, 8, 9), (3, 12, 1), (19, 19, 0).

25. Find the distance between the point (-1, 2, 3) and the plane x - y + z = 1.

26. Find the distance between the planes x - y = 3 and x - y = -1.

27. Find the distance between the skew lines $\langle -t, t-2, 3+2t \rangle$ and $\langle t, 3t-1, t-2 \rangle$.

- 28. Name the surface given by the equation $x y^2 + z^2 = 0$ and say where it's centered.
- 29. Name the surface given by the equation $2x^2 + y^2 + z^2 = 3$ and say where it's centered.
- 30. Name the surface given by the equation $-3z^2 3y^2 = -x^2$ and say where it's centered.
- 31. Name the surface given by the equation $x^2 2y + z^2 = 0$ and say where it's centered.
- 32. Name the surface given by the equation $x^2 y^2 z^2 = 5$ and say where it's centered.
- 33. Name the surface given by the equation $x^2 y^2 = 1 z^2$ and say where it's centered.
- 34. Sketch the trace of the surface $x^2 4y^2 + z^2 = 5$ when y = 1.

35. Convert the point (1, 1, 1) from rectangular to cylindrical coordinates.

36. Convert the point (1, 1, 1) from rectangular to spherical coordinates.

37. Convert the point $(2, \pi, -2)$ from cylindrical to rectangular coordinates.

38. Convert the point $\left(2, \frac{\pi}{2}, \frac{\pi}{4}\right)$ from spherical to rectangular coordinates.

39. Convert the equation $x^2 - y^2 - z^2 = 2$ into spherical coordinates.

40. Convert the equation $x^2 + 2y^2 + 2z^2 = 1$ into cylindrical coordinates.

41. Find the equation of the space curve in the intersection of the cylinder $x^2 + y^2 = 4$ and the plane z - x - y = 1

42. Calculate $\int_1^4 \langle t^2, e^t, \cos(t) \rangle \, dt.$

43. Calculate the derivative of $\langle e^t \sin(t^2), \ln(t), t^2 + 5t \rangle$.

44. Find the unit tangent vector to the curve $\langle e^t, t^2 + 5t, -\cos(t) \rangle$ when t = 0.

45. Find the equation of the tangent line(s) to the curve $\langle t^2, t^3, t \rangle$ at the point (4, 8, 2).

46. Find the angle of intersection of the curves $\langle t-1, t^2, 2 \rangle$ and $\langle -1, t, t^2 + 2 \rangle$.

47. Set up the integral to determine the arc length of the curve $\langle e^t, t^2, t^7 - 5t^2 \rangle$ from t = 4 to t = 8.

48. Reparametrize the curve $\langle \cos(t), \sin(t), 5t \rangle$ by arc length.

49. Parametrize a cylinder of radius 3 centered on the y-axis.

50. Parametrize a sphere of radius 2 centered at the origin.

51. Parametrize the plane 2x - y + 3z = -2.

52. Parametrize the cone $4x^2 + 2y^2 = z^2$.

53. Parametrize the ellipsoid $3x^2 + 5y^2 + z^2 = 1$.

54. Parametrize the elliptic paraboloid $y = 2z^2 + x^2$.

55. Parametrize the bottom hemisphere of a sphere with radius 10 centered at the origin.