

Sequences that converge to 0

Solution: cards labeled with multiples of two.

$$(2) \frac{5}{2n+1} \rightarrow 0$$

$$(4) \frac{e^n}{n!} \rightarrow 0$$

$$(8) \sin\left(\frac{1}{n}\right) \rightarrow 0$$

$$(16) \frac{(-1)^n n}{e^n} \rightarrow 0$$

$$(22) \frac{\sin n^2}{\sqrt{n}} \rightarrow 0$$

$$(26) \frac{(-1)^n n^4}{n!} \rightarrow 0$$

$$(34) \frac{n8^n}{3^{2n+1}} \rightarrow 0.$$

Sequences that converge, but not to 0

Solution: cards labeled with multiples of three.

$$(3) \cos\left(\frac{n}{n^2}\right) \rightarrow 1$$

$$(9) \left(1 + \frac{1}{n}\right)^n \rightarrow e$$

$$(27) \frac{\ln n}{\ln(n^2)} \rightarrow \frac{1}{2}$$

$$(33) \frac{\sqrt{n^2+1}}{3n-1} \rightarrow \frac{1}{3}.$$

Sequences that diverge to ∞

Solution: cards labeled with multiples of five.

$$(5) \frac{n}{\ln n} \rightarrow \infty$$

$$(25) \frac{10^n}{n5^n} \rightarrow \infty$$

$$(55) \frac{n^2}{n \ln n} \rightarrow \infty$$

$$(85) \frac{e^n}{\sqrt{n}} \rightarrow \infty.$$

Sequences that diverge, but not to ∞

Solution: cards labeled with multiples of seven.

$$(7) \frac{3n^3 + n}{1 - 4n^2} \rightarrow -\infty$$

$$(49) \frac{(-1)^n 2^n}{n^4} \text{ diverges, but not to } \pm\infty$$

$$(77) \frac{(-1)^n n^2}{n^2 + 1} \text{ diverges, but not to } \pm\infty.$$